



INDIAN SCHOOL AL WADI AL KABIR

Class XII, Mathematics **Worksheet- INTEGRALS- 2**

16-08-2020

Short answer type (2 marks)

Q.1.	Evaluate: $\int \frac{x^3 - x^2 + x - 1}{x - 1} dx$
Q.2.	Evaluate: $\int \left(\frac{1}{\sin^2 x \cdot \cos^2 x} \right) dx$
Q.3.	Evaluate: $\int \frac{2}{1 + \cos 2x} dx$
Q.4	Evaluate: $\int \frac{\cos 2x - \cos 2\alpha}{\cos x - \cos \alpha} dx$
Q.5	Evaluate: $\int \tan^{-1} \left(\sqrt{\frac{1 - \sin x}{1 + \sin x}} \right) dx$
Q.6	Evaluate: $\int \left(\frac{\sin x}{\sin(x + a)} \right) dx$
Q.7	Evaluate: $\int \frac{\sin x - x \cos x}{x(x + \sin x)} dx$
Q.8	Evaluate: $\int \left(\frac{x + \cos 6x}{3x^2 + \sin 6x} \right) dx$
Q.9	Evaluate: $\int \frac{\cos x}{(1 + \sin x)(2 + \sin x)} dx$
Q.10	Evaluate: $\int x \sqrt{x^4 - 1} dx$
Long answer type (4 marks)	
Q.11	Evaluate: $\int \frac{x^2 - 3x + 1}{\sqrt{1 - x^2}} dx$
Q.12	Evaluate: $\int \frac{1}{\log x} - \frac{1}{(\log x)^2} dx$
Q.13	Evaluate $\int \frac{1}{x^3(x^5 + 1)^{\frac{3}{5}}} dx$
Q.14	Evaluate $\int \frac{\sec x}{1 + 2\sin^2 x} dx$

Q.15	Evaluate $\int \frac{1}{\sin x + \sin 2x} dx$
Q.16	Evaluate: $\int (\sqrt{\tan x} + \sqrt{\cot x}) dx$
Q.17	Evaluate: $\int \frac{3x + 5}{x^3 - x^2 - x + 1} dx$
Q.18	Evaluate: $\int \sec^3 x dx$
Q.19	Evaluate: $\int \frac{(x - 5)e^x}{(x - 3)^3} dx$
Q.20	Evaluate $\int \frac{\sqrt{x^2 + 1}[\log(x^2 + 1) - 2\log x]}{x^4} dx$

Answers

1	$\frac{x^3}{3} + x + c$	2	$\tan x - \cot x + C$
3.	$\tan x + C$	4.	$2(\sin x + x \cos a) + c$
5	$\frac{\pi}{4}x - \frac{x^2}{2} + C$	6	$x \cos a - \sin a \log \sin(x + a) + c$
7	$\log \left \frac{x}{x + \sin x} \right + c$	8	$\frac{1}{6}(3x^2 + \sin 6x) + c$
9	$\log \left \frac{1 + \sin x}{2 + \sin x} \right + c$	10	$\frac{x^2}{2} \sqrt{x^4 - 1} + \frac{1}{2} \log x^4 + \sqrt{x^4 - 1} + C$
11	$-\frac{x}{2} \sqrt{1 - x^2} + \frac{3}{2} \sin^{-1} x + 3\sqrt{1 - x^2} + c$	12	$\frac{x}{\log x} + c$
13	$-\frac{1}{2} \left(1 + \frac{1}{x^5}\right)^{\frac{2}{5}} + c$	14	$\frac{1}{6} \log \left \frac{1 + \sin x}{1 - \sin x} \right + \frac{\sqrt{2}}{3} \tan^{-1}(\sqrt{2} \sin x) + c$
15	$\frac{1}{2} \log 1 + \cos x + \frac{1}{6} \log 1 - \cos x - \frac{2}{3} \log 1 + 2 \cos x + c$	16	$\sqrt{2} \sin^{-1}(\sin x - \cos x) + c$
17	$-\frac{1}{2} \log x - 1 - \frac{4}{x - 1} + \frac{1}{2} \log x + 1 + c$	18	$\frac{1}{2} (\sec x \tan x + \log \sec x + \tan x) + c$
19	$\frac{e^x}{(x - 3)^2} + c$	20	$-\frac{1}{3} \left(1 + \frac{1}{x^2}\right)^{\frac{3}{2}} \left[\log \left(1 + \frac{1}{x^2}\right) - \frac{2}{3} \right] + c$